# Boost Converter with Active Snubber Network 

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#### Abstract

A new concept for reducing the losses in a boost converter is described. With the help of an auxiliary switch and a resonant circuit, zero-voltage switching at turn-off and zerocurrent switching during turn-on are achieved. The modes of the circuit are shown in detail. The energy recovery of the turn-off is analyzed and the recovered energy is calculated; an optimized switching concept therefore is described. The influence of the parasitic capacity of the switch is discussed. Dimensioning hints for the converter and the design of the recuperation circuit are given. A bread-boarded design shows the functional efficiency of the concept.


Index Terms-snubbers, active circuits, switching converters, zero current switching, zero voltage switching.

## I. Introduction

There are numerous papers about the boost converter and methods to decrease the losses. Basics of the boost converter are described e.g. in [1, 2]. A very well-known method to reduce the losses is the quasi-resonant converter concept [3-5]. We distinguish zero-current ZC quasi-resonant and zerovoltage ZV quasi-resonant converters. Other concepts are the zero voltage and the zero current transition concept or combinations of them [6-24].

In this paper we use an active snubber concept, based on the network described in [21] to reduce the losses. The active switch turns on with zero current switching ZCS and turns off with zero voltage switching ZVS. The energy used for this soft switching is fed into the output by a recuperation circuit with low losses. The tasks of the snubber are: to reduce turn-off switching loss and to define the $\mathrm{dv} / \mathrm{dt}$ ratio during turn off. Due to new very fast active switching elements, the second one becomes more important (to reduce problems with EMC).

## II. Circuit Operation

The boost converter (Fig. 1) consists of the coil L, the active switch S , the free-wheeling diode D , and the output capacitor C . The snubber consists of the inductor $\mathrm{L}_{\mathrm{E}}$ (to reduce the velocity of the current during turn on), the capacitor $\mathrm{C}_{\mathrm{E}}$ (to reduce the losses across the switch S during turn off and to reduce the overvoltage across the switch), the snubber diode $\mathrm{D}_{\mathrm{E}}$, the diode $\mathrm{D}_{\mathrm{U}}$, the inductor $\mathrm{L}_{\mathrm{U}}$, the auxiliary switch $\mathrm{S}_{\mathrm{U}}$, and the feedback diode $\mathrm{D}_{\mathrm{R}}$ (to transfer the energy of the snubber capacitor $\mathrm{C}_{\mathrm{E}}$ to the output). The load is represented by a resistor. $\mathrm{U}_{\mathrm{in}}$ is the input voltage, $\mathrm{U}_{\text {out }}$ is the output voltage.

Inductance $L$ is large compared to $L_{E}$, capacitance $C$ is large compared to $\mathrm{C}_{\mathrm{E}}$. For the analysis, we replace the converter coil L by a current source I, and the output capacitor C by a voltage source $\mathrm{U}_{\text {out }}$. Ideal elements are used.

In following, the functioning of the proposed boost converter with active snubber network will be described.

We can make a distinction between different seven time intervals, which we called Modes.


Figure 1. Boost converter with low-loss snubber network.
Mode 0 (Fig. 2): the active switch is on, the capacitor $\mathrm{C}_{\mathrm{E}}$ is discharged. This is the normal on-state of the boost converter.


Figure 2. Turn-on state of the converter (mode 0).
Mode 1 (Fig. 3): at the beginning of this mode, the active switch S is turned off.


Figure 3. Start of the turn-off process (Mode 1).
The snubber diode $\mathrm{D}_{\mathrm{E}}$ turns on and the current commutates into the snubber capacitor $\mathrm{C}_{\mathrm{E}}$. The capacitor voltage $\mathrm{u}_{\mathrm{CE}}(\mathrm{t})$ increases linearly according to
$\frac{\mathrm{du}_{\mathrm{CE}}}{\mathrm{dt}}=\frac{\mathrm{I}}{\mathrm{C}_{\mathrm{E}}} ; \quad u_{\mathrm{CE}}(0)=0$
$u_{C E}(t)=\frac{I}{C_{E}} t$
until it reaches $\mathrm{U}_{\text {out }}$.
Mode 2 (Fig. 4): When the voltage across the capacitor $\mathrm{C}_{\mathrm{E}}$ reaches $\mathrm{U}_{\text {out }}$, the free-wheeling diode D turns on.

The energy in $\mathrm{L}_{\mathrm{E}}$ continues to be transferred into $\mathrm{C}_{\mathrm{E}}$ and a (little) part is now already transferred to the output. The circuit can be described by the state equations:


Figure 4. The free-wheeling diode turns on (Mode2).
$\frac{\mathrm{di}_{\mathrm{LE}}}{\mathrm{dt}}=\frac{\mathrm{U}_{\text {out }}-\mathrm{u}_{\mathrm{CE}}}{\mathrm{L}_{\mathrm{E}}} ; \quad \mathrm{i}_{\mathrm{LE}}(0)=\mathrm{I}$
$\frac{d i_{\text {LU }}}{d t}=\frac{u_{C E}-U_{\text {out }}}{L_{U}} ; \quad i_{L U}(0)=0$
$\frac{d u_{C E}}{d t}=\frac{i_{L E}-i_{L U}}{C_{E}} ; \quad u_{C E}(0)=U_{\text {out }}$
This leads to:
$\mathrm{i}_{\mathrm{LE}}(\mathrm{t})=\frac{\mathrm{L}_{\mathrm{E}}}{\mathrm{L}_{\mathrm{E}}+\mathrm{L}_{\mathrm{U}}} \mathrm{I}\left(1+\frac{\mathrm{L}_{\mathrm{U}}}{\mathrm{L}_{\mathrm{E}}} \cos \omega_{2} \mathrm{t}\right)$
$\mathrm{i}_{\mathrm{LU}}(\mathrm{t})=\frac{\mathrm{L}_{\mathrm{E}}}{\mathrm{L}_{\mathrm{E}}+\mathrm{L}_{\mathrm{U}}} \mathrm{I}\left(1-\cos \omega_{2} \mathrm{t}\right)$
$u_{C E}(t)=U_{2}+\frac{I}{\omega_{2} C_{E}} \sin \omega_{2} t$
where
$\omega_{2}=\sqrt{\frac{\mathrm{L}_{\mathrm{E}}+\mathrm{L}_{\mathrm{U}}}{\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}}}$.
Mode 2 ends when the current $\mathrm{i}_{\mathrm{LE}}$ reaches zero and the snubber diode $D_{E}$ turns off. The voltage across $C_{E}$ is now higher than the output voltage $\mathrm{U}_{\text {out }}$.

Mode 3 (Fig. 5): the capacitor $\mathrm{C}_{\mathrm{E}}$ and $\mathrm{L}_{\mathrm{U}}$ form a resonant circuit.


Figure 5. Resonance during the off-time (Mode 3).
If the voltage across $\mathrm{C}_{\mathrm{E}}$ gets lower than $\mathrm{U}_{\text {out }}$, the circuit goes again in Mode 2 with different initial conditions. There will be a ringing between these two modes until the voltage at $C_{E}$ is stabilized to $U_{\text {out }}$. The circuit is described by:

$$
\begin{equation*}
\frac{1}{\mathrm{C}_{\mathrm{E}}} \int_{0}^{\mathrm{t}} \mathrm{i}_{\mathrm{LU}} \cdot \mathrm{dt}-\mathrm{u}_{\mathrm{CE}}(0)+\mathrm{L}_{\mathrm{U}} \frac{\mathrm{di} \mathrm{i}_{\mathrm{LU}}}{\mathrm{dt}}+\mathrm{U}_{\text {out }}=0 \tag{10}
\end{equation*}
$$

where $u_{C E}(0)$ is the voltage across $C_{E}$ when Mode 3 begins.
Mode 4 (Fig. 6): this is the normal turn-off mode (freewheeling mode) of the converter.

Mode 5 (Fig. 7): the main switch S is turned on again.
The current through the main switch $S$ increases and the current through the free-wheeling diode D decreases
$\frac{\mathrm{di}_{\mathrm{LE}}}{\mathrm{dt}}=\frac{\mathrm{U}_{\text {out }}}{\mathrm{L}_{\mathrm{E}}} ; \quad \mathrm{i}_{\mathrm{LE}}(0)=0$


Figure 6. Turn-off state of the converter (Mode 4).
Mode 5 ends when the current $\mathrm{I}_{\mathrm{LE}}$ reaches I . Then the current in the free-wheeling diode D is zero and it turns off. The main switch is now carrying the current I .


Figure 7. Beginning of the turn-on process (Mode 5).
Mode 6 (Fig. 8): The main switch is now carrying the current I and the auxiliary switch $\mathrm{S}_{\mathrm{U}}$ is turned on (this switch can already be turned on synchronously to the main switch S, Mode 5).


Figure 8. Resonant discharge of the snubber capacitor (Mode 6).
The right part of the circuit is now described by
$\frac{\mathrm{di}_{\mathrm{LU}}}{\mathrm{dt}}=\frac{\mathrm{u}_{\mathrm{CE}}}{\mathrm{L}_{\mathrm{U}}} ; \quad \mathrm{i}_{\mathrm{LU}}(0)=0$
$\frac{\mathrm{du}_{\mathrm{CE}}}{\mathrm{dt}}=\frac{-\mathrm{i}_{\mathrm{LU}}}{\mathrm{C}_{\mathrm{E}}} ; \quad \mathrm{u}_{\mathrm{CE}}(0)=\mathrm{U}_{\text {out }}$
This leads to
$\mathrm{i}_{\mathrm{LU}}(\mathrm{t})=\mathrm{U}_{\text {out }} \omega_{6} \mathrm{C}_{\mathrm{E}} \sin \omega_{6} \mathrm{t}$
$u_{\text {CE }}(t)=U_{\text {out }} \cos \omega_{6} t$
where
$\omega_{6}=\left(\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}\right)^{-1 / 2}$
The capacitor $\mathrm{C}_{\mathrm{E}}$ is discharged within a quarter of the period and the current reaches its maximum $\mathrm{I}_{\text {LUmax }}$ (Fig. 9):
$\mathrm{I}_{\text {LUmax }}=\mathrm{U}_{2} \omega_{6} \mathrm{C}_{\mathrm{E}}$
The duration of this process is:
$\mathrm{T}_{6}=\frac{\pi}{2} \sqrt{\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}}=\frac{\pi}{2} \frac{1}{\omega_{6}}$
The capacitor voltage $u_{\text {CE }}$ is now clamped to zero due to the snubber diode $\mathrm{D}_{\mathrm{E}}$. To feed back the energy, the auxiliary switch $\mathrm{S}_{\mathrm{U}}$ has to be turned off.


Figure 9. Current through the inductor $\mathrm{L}_{\mathrm{U}}$ and voltage across the snubber capacitor $\mathrm{C}_{\mathrm{E}}$ during Mode 6 .

Mode 7 (Fig. 10): auxiliary switch $\mathrm{S}_{\mathrm{U}}$ has turned off.


Figure 10. Recuperation (Mode 7).
The current $\mathrm{i}_{\mathrm{LU}}$ decreases until the diodes turn off when the current reaches zero
$\frac{\mathrm{di}_{\mathrm{LU}}}{\mathrm{dt}}=\frac{-\mathrm{U}_{\text {out }}}{\mathrm{L}_{\mathrm{U}}} ; \quad \mathrm{i}_{\mathrm{LU}}(0)=\mathrm{I}_{\mathrm{LU} \max }$
The current decreases linearly according to
$\mathrm{i}_{\mathrm{LU}}(\mathrm{t})=\frac{\mathrm{U}_{\text {out }}}{\mathrm{L}_{\mathrm{U}}}\left(\sqrt{\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}}-\mathrm{t}\right)$
The time for demagnetizing the inductor $\mathrm{L}_{\mathrm{U}}$ is
$\mathrm{T}_{7}=\sqrt{\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}}=\frac{1}{\omega_{7}}=\frac{1}{\omega_{6}}$
When $i_{L U}$ reaches zero, the diodes of the snubber network turn off. The time necessary to feed back the stored energy is therefore
$\mathrm{T}_{6}+\mathrm{T}_{7}=\left(\frac{\pi}{2}+1\right) \sqrt{\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}}=\left(\frac{\pi}{2}+1\right) \mathrm{T}_{7}$
Now the circuit is again in Mode 0 !

## III. Energy Recovery for the Turn-off Snubber

After turn off of the main switch S , the snubber capacitor $C_{E}$ is charged to the output voltage $U_{\text {out }}$. At the begin of Mode 6 (or also Mode 5, but that is not important), the energy stored in $\mathrm{C}_{\mathrm{E}}$ is
$\mathrm{W}_{\mathrm{CE}}=\frac{\mathrm{C}_{\mathrm{E}} \mathrm{U}_{\text {out }}^{2}}{2}$.
Using a dissipative snubber this energy has to be dissipated in a resistor $R_{E}$. Then, with the switching frequency f , the loss would be

$$
\begin{equation*}
\mathrm{P}_{\mathrm{RE}}=\frac{\mathrm{C}_{\mathrm{E}} \mathrm{U}_{\text {out }}^{2}}{2} \mathrm{f} \tag{24}
\end{equation*}
$$

When the main switch S turns on again, the auxiliary switch $\mathrm{S}_{\mathrm{U}}$ can be turned on as well (Mode 6). The capacitor $C_{E}$ is discharged within a quarter of the period and the
current reaches its maximum $\mathrm{I}_{\text {LUmax }}$ (Fig. 9). According Fig. 8, the circuit can be described by

$$
\begin{equation*}
\mathrm{L}_{\mathrm{U}} \frac{\mathrm{~d} \mathrm{i}_{\mathrm{LU}}}{\mathrm{dt}}+\frac{1}{\mathrm{C}_{\mathrm{E}}} \int_{0}^{\mathrm{t}} \mathrm{i}_{\mathrm{LU}} \mathrm{dt}-\mathrm{U}_{\text {out }}+\mathrm{V}_{\mathrm{D}}+\mathrm{R}_{\text {loss1 }} \mathrm{i}_{\mathrm{LU}}=0 . \tag{25}
\end{equation*}
$$

where $V_{D}$ is the knee voltage of the diode $D_{U}$ and $R_{\text {loss1 }}$ is the series equivalent resistance of the inductor $\mathrm{L}_{U}$ and of the capacitor $\mathrm{C}_{\mathrm{E}}$, resistances, the differential resistance of the diode $\mathrm{D}_{\mathrm{U}}$ and the on-state resistance of the auxiliary switch $\mathrm{S}_{\mathrm{U}}$. Therefore, the current can be described by

$$
\begin{equation*}
\mathrm{i}_{\mathrm{LU}}(\mathrm{t})=\left(\mathrm{U}_{\mathrm{out}}-\mathrm{V}_{\mathrm{D}}\right) \cdot \alpha_{1} \cdot \sin \omega_{1} \mathrm{t} \tag{26}
\end{equation*}
$$

where
$\alpha_{1}=2 \sqrt{\frac{C_{E}}{4 \mathrm{~L}_{\mathrm{U}}-\mathrm{R}_{\text {loss1 }}^{2} \mathrm{C}_{\mathrm{E}}}} ; \quad \omega_{1}=\sqrt{\frac{1}{\mathrm{~L}_{\mathrm{U}} \mathrm{C}_{\mathrm{E}}}-\frac{\mathrm{R}_{\text {loss1 }}^{2}}{4 \mathrm{~L}_{\mathrm{U}}^{2}}}$
The capacitor $\mathrm{C}_{\mathrm{E}}$ is completely discharged, when the current reaches its maximum at $\mathrm{T}_{\mathrm{x}}$ :
$\mathrm{T}_{\mathrm{x}}=\frac{\pi}{2} \frac{1}{\omega_{1}}$
The loss energy can be calculated by
$W_{\text {loss1 }}=\int_{0}^{T_{\mathrm{x}}} R_{\text {loss1 }} i_{\text {LU }}^{2}(t) \cdot d t$
$\mathrm{W}_{\text {loss1 }}=\mathrm{R}_{\text {loss1 }}\left(\mathrm{U}_{\text {out }}-\mathrm{V}_{\mathrm{D}}\right)^{2} \alpha_{1}^{2} \frac{\mathrm{~T}_{\mathrm{x}}}{2}$.
Now, the diode $\mathrm{D}_{\mathrm{E}}$ turns on (Mode 7) and the voltage across $\mathrm{C}_{\mathrm{E}}$ is clamped. According Fig. 10, the circuit can be described by

$$
\begin{equation*}
\mathrm{L}_{\mathrm{U}} \frac{\mathrm{di} \mathrm{i}_{\mathrm{LU}}}{\mathrm{dt}}+3 \mathrm{~V}_{\mathrm{D}}+\mathrm{R}_{\text {loss } 2} \mathrm{i}_{\mathrm{LU}}+\mathrm{U}_{\text {out }}=0 \tag{31a}
\end{equation*}
$$

with initial condition:

$$
\begin{equation*}
\mathrm{i}_{\mathrm{LU}}(0)=\mathrm{i}_{\mathrm{LU}}\left(\mathrm{~T}_{\mathrm{x}}\right)=\left(\mathrm{U}_{\mathrm{out}}-\mathrm{V}_{\mathrm{D}}\right) \alpha_{1} \tag{31b}
\end{equation*}
$$

where $V_{D}$ is the knee voltage of the diodes $D_{E}, D_{U}$, and $D_{R}$, and $R_{\text {loss } 2}$ is the series equivalent resistance of the circuit consisting of the inductor $\mathrm{L}_{\mathrm{U}}$, the diodes $\mathrm{D}_{\mathrm{E}}, \mathrm{D}_{\mathrm{U}}$, and $\mathrm{D}_{\mathrm{R}}$ and the main switch S .

Solving the differential equation leads to

$$
\begin{equation*}
\mathrm{i}_{\mathrm{LU}}(\mathrm{t})=-\mathrm{I}_{\infty}+\mathrm{I}_{1} \exp \left(-\frac{\mathrm{t}}{\tau}\right) \tag{32}
\end{equation*}
$$

where
$\mathrm{I}_{\infty}=\frac{\mathrm{U}_{2}+3 \mathrm{~V}_{\mathrm{D}}}{\mathrm{R}_{\text {loss2 }}} ; \quad \mathrm{I}_{1}=\mathrm{i}_{\mathrm{LU}}(0)+\mathrm{I}_{\infty} ; \quad \tau=\frac{\mathrm{L}_{\mathrm{U}}}{\mathrm{R}_{\text {loss } 2}}$
The current decreases and reaches zero after $\mathrm{T}_{\mathrm{y}}$ :
$\mathrm{T}_{\mathrm{y}}=\tau \ln \left(\frac{\mathrm{I}_{1}}{\mathrm{I}_{\infty}}\right)$.
Now, the diodes turn off and the recuperation ends. The loss energy during Mode 7 can be calculated by

$$
\begin{align*}
& \mathrm{W}_{\text {loss } 2}=\int_{0}^{\mathrm{T}_{\mathrm{y}}} \mathrm{R}_{\text {loss } 2} \mathrm{i}_{\mathrm{LU}}^{2}(\mathrm{t}) \cdot \mathrm{dt}  \tag{35}\\
& \mathrm{~W}_{\text {loss } 2}=\mathrm{R}_{\text {loss } 2}\left[\mathrm{I}_{\infty}^{2} \cdot \mathrm{~T}_{\mathrm{y}}+2 \mathrm{I}_{\infty} \mathrm{I}_{1} \beta \tau+\mathrm{I}_{1}^{2} \beta \frac{\tau}{2}\right] \tag{36}
\end{align*}
$$

where

$$
\begin{equation*}
\beta=\frac{\mathrm{U}_{\text {out }}+3 \mathrm{~V}_{\mathrm{D}}}{\mathrm{R}_{\text {loss } 2} \mathrm{i}_{\mathrm{LU}}(0)+\mathrm{U}_{2}+3 \mathrm{~V}_{\mathrm{D}}}-1=-\frac{\mathrm{i}_{\mathrm{LU}}(0)}{\mathrm{I}_{1}} \tag{37}
\end{equation*}
$$

Therefore, the losses of the recuperation network are

$$
\begin{equation*}
P_{\text {loss,rek }}=\mathrm{f}\left(\mathrm{~W}_{\text {loss } 1}+\mathrm{W}_{\text {loss } 2}\right) . \tag{38}
\end{equation*}
$$

The recovered power which can be fed back $P_{\text {back }}$ is
$P_{\text {back }}=f\left[\frac{\mathrm{C}_{\mathrm{E}} \mathrm{U}_{\text {out }}^{2}}{2}-\left(\mathrm{W}_{\text {loss } 1}+\mathrm{W}_{\text {loss } 2}\right)\right]$.
This calculation is comprehensive. To get a rough overview we can make some approximations.

## IV. Approximate Estimation of the Fed Back Energy

For approximating the energy which is fed back, we use the idealized curves according (14), (18), (20), and (21) and we calculate the losses at the parasitic resistors. The knee voltage of the diodes shall be neglected, because it is small compared to the output voltage. With (14), and (18), for the loss energy during Mode 6 one can write

$$
\begin{equation*}
W_{\text {loss } 1}=\int_{0}^{T_{6}} R_{\text {loss1 }}\left[U_{\text {out }} \omega_{6} C_{E} \sin \left(\omega_{6} t\right)\right]^{2} d t . \tag{40}
\end{equation*}
$$

One gets

$$
\begin{equation*}
\mathrm{W}_{\text {loss1 }}=\frac{\pi}{4} \mathrm{U}_{\mathrm{out}}^{2} \mathrm{R}_{\text {loss1 }} \sqrt{\frac{\mathrm{C}_{\mathrm{E}}}{\mathrm{~L}_{\mathrm{U}}}} \mathrm{C}_{\mathrm{E}} \tag{41}
\end{equation*}
$$

During Mode 7, with (20) and (22), one can write for the loss energy

$$
\begin{align*}
& \mathrm{W}_{\text {loss } 2}=\int_{0}^{\mathrm{T}_{7}} \mathrm{R}_{\text {loss } 2} \frac{\mathrm{U}_{\mathrm{out}}^{2}}{\mathrm{~L}_{\mathrm{U}}^{2}}\left(\mathrm{~T}_{7}-\mathrm{t}\right)^{2} \mathrm{dt}  \tag{42}\\
& \mathrm{~W}_{\text {loss } 2}=\frac{1}{3} \mathrm{U}_{\mathrm{out}}^{2} \mathrm{R}_{\text {loss } 2} \sqrt{\frac{\mathrm{C}_{\mathrm{E}}}{\mathrm{~L}_{\mathrm{U}}}} \mathrm{C}_{\mathrm{E}}
\end{align*}
$$

The losses of the recuperation network can be approximated by:

$$
\begin{equation*}
\mathrm{P}_{\text {loss }}=\mathrm{f} \cdot \mathrm{U}_{\text {out }}^{2} \sqrt{\frac{\mathrm{C}_{\mathrm{E}}}{\mathrm{~L}_{\mathrm{U}}}} \mathrm{C}_{\mathrm{E}}\left(\frac{\pi}{4} \mathrm{R}_{\text {loss1 }}+\frac{1}{3} \mathrm{R}_{\text {loss } 2}\right) \tag{44}
\end{equation*}
$$

Considering the same equivalent loss resistance for both modes, the recovered power $\mathrm{P}_{\text {back }}$ can be expressed as:

$$
\begin{equation*}
\mathrm{P}_{\text {back }}=\mathrm{f} \cdot \frac{\mathrm{C}_{\mathrm{E}} \mathrm{U}_{\text {out }}^{2}}{2}\left(1-2.23 \mathrm{R}_{\text {loss }} \sqrt{\frac{\mathrm{C}_{\mathrm{E}}}{\mathrm{~L}_{\mathrm{U}}}}\right) . \tag{45}
\end{equation*}
$$

With the image impedance of the resonant circuit

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{U}}=\sqrt{\frac{\mathrm{L}_{\mathrm{U}}}{\mathrm{C}_{\mathrm{E}}}} \tag{46}
\end{equation*}
$$

we can write now:

$$
\begin{equation*}
\mathrm{P}_{\text {back }}=\mathrm{f} \cdot \frac{\mathrm{C}_{\mathrm{E}} \mathrm{U}_{\text {out }}^{2}}{2}\left(1-2.23 \frac{\mathrm{R}_{\text {loss }}}{\mathrm{Z}_{\mathrm{U}}}\right) . \tag{47}
\end{equation*}
$$

The image impedance of the resonant circuit $Z_{U}$ is large compared to $\mathrm{R}_{\text {loss }}$, therefore a large amount of the stored energy of the snubber capacitor can be fed into the output of the converter.

## V. Optimized Control of the Recuperation

A little bit more efficient way to control the recuperation network is to turn off the auxiliary switch $\mathrm{S}_{\mathrm{U}}$ at the moment when the voltage across the capacitor $\mathrm{C}_{\mathrm{E}}$ has such a value, that the capacitor will be completely discharged when the current $i_{\text {LU }}$ reaches zero and the diodes turn off.

When the auxiliary switch is turned off after $\mathrm{T}_{\mathrm{z}}$, then, according to (14) and (15), the current in $\mathrm{L}_{\mathrm{U}}$ and the voltage
across $\mathrm{C}_{\mathrm{E}}$ are, respectively:
$\mathrm{i}_{\mathrm{LU}}\left(\mathrm{T}_{\mathrm{z}}\right)=\mathrm{U}_{\text {out }} \omega_{6} \mathrm{C}_{\mathrm{E}} \sin \omega_{6} \mathrm{~T}_{\mathrm{z}}$
$\mathrm{u}_{\mathrm{CE}}\left(\mathrm{T}_{\mathrm{z}}\right)=\mathrm{U}_{\text {out }} \cos \omega_{6} \mathrm{~T}_{\mathrm{z}}$.
If the auxiliary switch is turned off after
$\mathrm{T}_{\mathrm{z}}=\frac{\pi}{3} \sqrt{\mathrm{C}_{\mathrm{E}} \mathrm{L}_{\mathrm{U}}}=\frac{\pi}{3} \mathrm{~T}_{7}$,
the mode that follows is described by KVL according to:

$$
\begin{equation*}
\mathrm{L}_{\mathrm{U}} \frac{\mathrm{di}_{\mathrm{LU}}}{\mathrm{dt}}+\mathrm{U}_{\mathrm{out}}+\frac{1}{\mathrm{C}_{\mathrm{E}}} \int_{0}^{\mathrm{t}} \mathrm{i}_{\mathrm{LU}} \mathrm{dt}=\mathrm{u}_{\mathrm{CE}}\left(\mathrm{~T}_{\mathrm{Z}}\right) \tag{51}
\end{equation*}
$$

with initial conditions:
$\mathrm{i}_{\mathrm{LU}}\left(\mathrm{T}_{\mathrm{Z}}\right)=\mathrm{i}_{\mathrm{LU}}\left(\frac{\pi}{3} \mathrm{~T}_{7}\right)=\frac{\sqrt{3}}{2} \mathrm{U}_{\text {out }} \omega_{6} \mathrm{C}_{\mathrm{E}}$
$\mathrm{u}_{\mathrm{CE}}\left(\mathrm{T}_{\mathrm{z}}\right)=\mathrm{u}_{\mathrm{CE}}\left(\frac{\pi}{3} \mathrm{~T}_{7}\right)=\frac{1}{2} \mathrm{U}_{\text {out }}$.
Solving the differential equation leads to:
$i_{L U}(t)=u_{a} \sqrt{\frac{C_{E}}{L_{U}}}\left(\sin \omega_{6} t\right)+i_{L U}\left(T_{z}\right)\left(\cos \omega_{6} t\right)$
$u_{C E}(t)=+u_{C E}\left(T_{z}\right)-u_{a}\left(1-\cos \omega_{6} t\right)-i_{L U}\left(T_{z}\right) \sqrt{\frac{L_{U}}{C_{E}}}\left(\sin \omega_{6} t\right)$
with
$\mathrm{u}_{\mathrm{a}}=\mathrm{u}_{\mathrm{CE}}\left(\mathrm{T}_{\mathrm{z}}\right)-\mathrm{U}_{\text {out }}$.
The voltage across $\mathrm{C}_{\mathrm{E}}$ and the current through the inductor $\mathrm{L}_{\mathrm{U}}$ are zero after

$$
\begin{equation*}
\mathrm{T}_{\mathrm{z}}=\frac{\pi}{3} \sqrt{\mathrm{C}_{\mathrm{E}} \mathrm{~L}_{\mathrm{U}}}=\frac{\pi}{3} \mathrm{~T}_{7} \tag{57}
\end{equation*}
$$

Due to the fact that the current is smaller, the losses are a little bit smaller too. The auxiliary switch has to be turned off when the voltage across the snubber capacitor is half of the output voltage. This can be detected by a comparator. It makes especially sense when the capacitor is not overcharged. To avoid ringing when a turn-on inductor $L_{E}$ is used, a switch in series to $\mathrm{L}_{\mathrm{E}}$ can be included leading to modifications shown also in [15]. This reduces ringing during turn-off and enables an optimal feed-back of the energy, when the snubber capacitor is overcharged. This will be shown in a future paper.

## VI. Influence of the Parasitic Capacitor of the Active Switch

In previous chapters, we studied only the main effect and used only the parameters $\mathrm{L}_{\mathrm{E}}, \mathrm{D}_{\mathrm{E}}$, and $\mathrm{C}_{\mathrm{E}}$ of the network. When the voltage across the switch reaches the output voltage $\mathrm{U}_{\text {out }}$, the free-wheeling diode D turns on. Considering the circuit consisting of the parasitic capacitance of the active switch $\mathrm{C}_{\mathrm{S}}$, the snubber capacitor $\mathrm{C}_{\mathrm{E}}$, and the snubber inductor $L_{E}$ we get for the current $i_{L E}$, the current in the main diode D , and the voltage across the switch

$$
\begin{align*}
& i_{L E}(t)=I \cdot \cos \sqrt{\frac{1}{\left(C_{E}+C_{S}\right) L_{E}}} \cdot t  \tag{58}\\
& i_{D}(t)=I-i_{L E}(t)=I \cdot\left(1-\cos \sqrt{\frac{1}{\left(C_{E}+C_{S}\right) L_{E}}} \cdot t\right) \tag{59}
\end{align*}
$$

$u_{S}(t)=I \sqrt{\frac{L_{E}}{C_{E}+C_{S}}} \cdot \sin \sqrt{\frac{1}{\left(C_{E}+C_{S}\right) L_{E}}} \cdot t+U_{2}$.
The overshot is reduced to
$\Delta u_{S}=I \sqrt{\frac{L_{E}}{C_{E}+C_{S}}}$.
The snubber diode $D_{E}$ turns off and there is now a ringing between $L_{E}$ and $C_{S}$ with the frequency

$$
\begin{equation*}
\mathrm{f}_{\mathrm{R}}=\frac{1}{2 \pi} \cdot \sqrt{\frac{1}{\mathrm{C}_{\mathrm{S}} \mathrm{~L}_{\mathrm{E}}}} \tag{62}
\end{equation*}
$$

and with the reduced amplitude $\Delta \mathrm{u}_{\mathrm{S}}$.
One can see, that the inductor $\mathrm{L}_{\mathrm{E}}$ should be dimensioned as small as possible when the presented low-loss snubber concept is used.

## VII. Design Equations

## A. Dimensioning of the basic boost converter

The boost converter shall transform a 50 V input voltage into an output voltage of 150 V . The rated power is 500 W . The output ripple shall be about $3 \%$. The mean value of the input current is therefore 10 A (omitting the losses). The current ripple is chosen to 5 A . The inductor can be determined by the basic equation of the inductor with the input voltage $U_{i n}$, the on-time of the active switch $d_{c} T$ (with $d_{c}$ as the duty cycle and T as the switching period), and the current ripple $\Delta \mathrm{I}$
$\mathrm{L}=\frac{\mathrm{U}_{\mathrm{in}} \cdot \mathrm{d}_{\mathrm{c}} \mathrm{T}}{\Delta \mathrm{I}}=\frac{\mathrm{U}_{1} \cdot \mathrm{~d}_{\mathrm{c}}}{\Delta \mathrm{I} \cdot \mathrm{f}}$
To get an approximate value for the output capacitor C we use the fact that during the on-time of the active switch the load has to be supplied by the capacitor. Therefore, the voltage across it decreases by $\Delta U_{C}$. We get
$\mathrm{C}=\frac{\mathrm{I}_{\text {Load }} \cdot \mathrm{d}_{\mathrm{c}} \mathrm{T}}{\Delta \mathrm{U}_{\mathrm{C}}}=\frac{\mathrm{I}_{\text {Load }} \cdot \mathrm{d}_{\mathrm{c}}}{\Delta \mathrm{U}_{\mathrm{C}} \cdot \mathrm{f}}$
This equation is derived for an ideal capacitor. In real cases, there is always a series resistor, which causes an additional voltage drop. So the value must be always chosen higher. With a chosen switching frequency of $\mathrm{f}=50 \mathrm{kHz}$ and an average output current of $\mathrm{I}_{\text {Load }}=3,3 \mathrm{~A}$ one gets $\mathrm{L}=130 \mu \mathrm{H}$, and $\mathrm{C}=33 \mu \mathrm{~F}$.

## B. Dimensioning of the snubber network

To reduce the losses during turn-on an inductor $\mathrm{L}_{\mathrm{E}}$ is connected in series with the active switch S . This defines the rise of current through the switch (and also the velocity of the current reduction in the diode D and therefore defines the reverse recovery peak). For a chosen value of the current rise $(\mathrm{di} / \mathrm{dt})_{\text {chosen }}$ we get
$L_{\mathrm{E}}=\frac{\mathrm{U}_{2}}{(\mathrm{di} / \mathrm{dt})_{\text {chosen }}}$
With $(\mathrm{di} / \mathrm{dt})_{\text {chosen }}=100 \mathrm{~A} / \mu \mathrm{s}$ and an output voltage of 150 V , one gets $\mathrm{L}_{\mathrm{E}}=1,5 \mu \mathrm{H}$.
The snubber capacitor $\mathrm{C}_{\mathrm{E}}$ has to limit the overvoltage during turn off caused by the inductor $\mathrm{L}_{\mathrm{E}}$ (and to limit the rise of the voltage across the switch). The energy stored into $\mathrm{L}_{\mathrm{E}}$ at the moment before turning off when the instantaneous current is I can be expressed as:
$\mathrm{W}_{\mathrm{LE}}=\frac{\mathrm{L}_{\mathrm{E}} \cdot \mathrm{I}^{2}}{2}$
This energy has to be charged into the capacitor $\mathrm{C}_{\mathrm{E}}$ when the voltage across it reaches $\mathrm{U}_{2}$ and the free-wheeling diode turns on (not considering the possible current path over $\mathrm{L}_{\mathrm{U}}$ ). Due to the delayed commutation into the free-wheeling diode further energy is transferred into the snubber capacitor $C_{E}$. With a chosen value of the overvoltage $(\Delta U)_{\text {chosen }}$ one gets:
$\mathrm{C}_{\mathrm{E}}=\frac{\mathrm{I}^{2}}{(\Delta \mathrm{U})_{\text {chosen }}^{2}} \mathrm{~L}_{\mathrm{E}}$.
With $\mathrm{I}=12 \mathrm{~A}$ and $(\Delta \mathrm{U})_{\text {chosen }}=50 \mathrm{~V}$, we obtained $\mathrm{C}_{\mathrm{E}}=81 \mathrm{nF}$.

With (22) it results
$L_{U}=\left(T_{6}+T_{7}\right)^{2} \frac{4}{(2+\pi)^{2} C_{E}}$
So $\left(\mathrm{T}_{6}+\mathrm{T}_{7}\right)$ must be smaller than the on-time of the active switch to ensure that the energy is completely fed back
$\left(\mathrm{T}_{1}+\mathrm{T}_{2}\right)<\mathrm{T}_{\mathrm{on}}=\mathrm{d}_{\mathrm{c}} \mathrm{T}$
For the simulation, we used $\mathrm{L}_{\mathrm{U}}=300 \mu \mathrm{H}$.

## VIII. Results

A simulation was performed by LT-Spice and a small converter was bread-boarded. The results show a good conformity with the theory. Fig. 11 shows the control signal of the main switch, the control signal of the auxiliary switch, the voltage across the snubber capacitor $\mathrm{C}_{\mathrm{E}}$, and the current through the inductor $\mathrm{L}_{\mathrm{U}}$.


Figure 11. Control signal of the main switch, control signal of the auxiliary switch, voltage across snubber capacitor $\mathrm{C}_{\mathrm{E}}$, and current through the inductor $\mathrm{L}_{\mathrm{U}}$ (top to down).

In Fig. 12, the control signals and the current through the main inductor, and the input current of the converter are shown.


Figure 12. Control signal of the main switch, control signal of the auxiliary switch, current through the main inductor L , and input current (top to down).

The input current is nearly constant due to a capacitor between the input connectors.

## IX. Conclusion

A boost converter with zero voltage turn-off and zerocurrent turn-on of the main switch was presented. With the help of a resonant circuit, two diodes and an auxiliary switch the energy stored in the snubber capacity is transferred to the output. To avoid ringing when a turn-on inductor $\mathrm{L}_{\mathrm{E}}$ is used, a switch in series to $\mathrm{L}_{\mathrm{E}}$ can be included leading to modifications. This reduces ringing during turn-off and enables an optimal feed-back of the energy, when the snubber capacitor is overcharged. The proposed circuit improves the efficiency if a snubber is necessary, e.g. because of EMC problems, and then it has a better efficiency compared to a converter with RCD snubber. The converter is useful for solar application, battery chargers and so on.

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